## Maths Reasoning Activity Area and Perimeter

## Warming up*

## Q1.

Here are five triangles on a square grid.


Four of the triangles have the same area.
Which triangle has a different area?

Q2.
Here is a set of 20 squares around a shaded space.


What is the area of the shaded space?


Q3.
A white square is painted in one corner of a grey square.
Each side of the white square is half the length of a side of the grey square.


## Not actual size

What is the area of the grey section?


Q4.
Draw a rectangle on the grid that has half the area of the shaded triangle.
Use a ruler.


Q5.
The perimeter of a square is 72 centimetres.


## Not actual size

The square is cut in half to make two identical rectangles.


What is the perimeter of one rectangle?


Q6.


Not actual size
The perimeter of this rectangle is 50 centimetres.
Calculate the length of the rectangle.


## Q7.

The following quadrilaterals all have a perimeter of $36 \mathbf{c m}$.
Here is a table to show the length of each side.

Complete the table.
One quadrilateral is done for you.

|  | Side lengths |  |  |  |
| :--- | :--- | :--- | :--- | :--- |
| square | 9 cm | 9 cm | 9 cm | 9 cm |
| rectangle | 3 cm |  |  |  |
| rhombus | 9 cm |  |  |  |
| kite | 10 cm |  |  |  |

Q8.
Megan says,
'If two rectangles have the same perimeter, they must have the same area.'

Is she correct?
Circle Yes or No.

Explain how you know.


1 mark

## Feeling more confident **

## Q1.

Here is a centimetre square grid.
On the grid draw a shape which has an area of 10 square centimetres.


On the grid below draw a rectangle which has a perimeter of $\mathbf{1 0}$ centimetres.


Q2.
The grid below is made of right-angled triangles like this:


Shade triangles on the grid to make a quadrilateral.



Q3.
Here are some shapes on a 1 cm square grid.

|  |  |  |  |  |  |  |  |  |  |  |  |  |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |  | B |  |  |  |  |  |  |
|  | A |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  | $C$ |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  | D |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  | $E$ |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  |  |  |  |  |  |  |

What is the perimeter of shape A?

Write the letter of the shape that has the smallest area.

Q4.
Here is a grid of regular hexagons.
The shaded shape has an area of 3 hexagons and a perimeter of 14 cm .
Draw another shape on the grid which has an area of 4 hexagons and a perimeter of 14 cm .


## Ready for a challenge ${ }^{* * *}$

Q1.
Here is an equilateral triangle inside a square.


## Not actual size

The perimeter of the triangle is 48 centimetres.
What is the perimeter of the square?


Q2.

An isosceles triangle has a perimeter of 12 cm .
One of its sides is 5 cm .
What could the length of each of the other two sides be?
Two different answers are possible.
Give both answers.


Q3.

A field measures 89.5 m by 60 m .

> 89.5m


What is the perimeter of the field?


1 mark

Q4.
Here are some shapes on a grid.


Which shape has the longest perimeter?

1 mark
Which shape has the largest area?


1 mark

Q5.
Alfie has some rectangles.


Not actual size

He makes this shape using three of the rectangles.


What is the perimeter of Alfie's shape?


2 marks

## Q6.

This plan of a garden is made of rectangles and triangles.
The area of each rectangle is $\mathbf{1 2}$ square metres.
What is the area of the whole garden?


The perimeter of the garden is $\mathbf{3 4}$ metres.
What is the length of the longest side of each triangle?



## Maths Reasoning Activity - Area and perimeter

## Answers

## Warming up*

## Q1.

A

> Accept alternative unambiguous positive indications of the correct triangle, e.g. $2 \frac{1}{2}$ or 2.5 .

Q2.

Accept $11 \mathrm{~cm}^{2}$

Q3.
Award TWO marks for the correct answer of 108
If the answer is incorrect, award ONE mark for evidence of appropriate method, eg
$12 \times 12=144$
$\frac{3}{4}$ of 144
OR
$(12 \times 12)-(6 \times 6)$
OR
$(12 \times 12)+(6 \times 6)$
OR
$(6 \times 6) \times 3$
Answer need not be obtained for the award of ONE mark.
Up to 2 (U1)

Q4.
A rectangle with area $6 \mathrm{~cm}^{2}$
A rectangle must be drawn but need not be shaded.

## Q5.

Award TWO marks for the correct answer of 54
If the answer is incorrect, award ONE mark for evidence of appropriate method, eg:

- $72 \div 4=18$
$18 \div 2=9$
$(18 \times 2)+(9 \times 2)$
OR
- $72 \div 4 \times 3$

Answer need not be obtained for the award of ONE mark.
Up to 2 (U1)

## Q6.

Award TWO marks for the correct answer of 18
If the answer is incorrect, award ONE mark for evidence of appropriate working, eg
$50 \div 2=25$
25-7 = wrong answer

## OR

$7 \times 2=14$
$50-14=36$
$36 \div 2=$ wrong answer
Working must be carried through to reach an answer for the award of ONE mark.

Q7.
Completes all three rows correctly, eg:

| rectangle | 3 cm | 3 cm | 15 c <br> m | 15 c <br> m |
| :---: | :---: | :---: | :---: | :---: |
| rhombus | 9 cm | 9 cm | 9 cm | 9 cm |
| kite | 10 c <br> m | 10 c <br> m | 8 cm | 8 cm |

## ! Measures

Accept Side lengths in each row may be given in any order
Accept correct values with cm omitted eg, for the rectangle:

- $15 \quad 3 \quad 15$
or
Completes two rows correctly

Q8.
Indicates No and gives a correct explanation that includes indicating two different areas, eg:

- A rectangle with sides 6 cm by 2 cm has a perimeter of 16 cm and an area of $12 \mathrm{~cm}^{2}$ but a rectangle with sides 5 cm and 3 cm has the same perimeter of 16 cm but it has an area of $15 \mathrm{~cm}^{2}$ which is different so she is not correct
- A square with sides 3 cm by 3 cm and a rectangle with sides 4 cm by 2 cm have the same perimeter of 12 cm but they have different areas of $9 \mathrm{~cm}^{2}$ and $8 \mathrm{~cm}^{2}$

Accept minimally acceptable explanation, eg:

- $6 \times 2=12,5 \times 3=15$
- 



7


8
! Ignore any incorrect units given in an otherwise correct explanation, eg:

- $6^{2}$ for $6 \mathrm{~cm}^{2}$
! Indicates Yes, or no decision made, but explanation clearly correct
Condone, provided the explanation is more than minimal
Do not accept Incomplete or incorrect explanation, eg.
- $6 \times 2,5 \times 3$
- Two rectangles, one with sides 6 cm by 5 cm and one with sides 8 cm by 3 cm have the same perimeter of 22 cm but they don't have the same area
- 



7


8

## Feeling more confident**

## Q1.

(a) Any shape with an area of $10 \mathrm{~cm}^{2}$, eg


The shape need not be aligned with the grid.
Accept slight inaccuracies in drawing provided intention is clear.
(b) Any rectangle with a perimeter of 10 cm , eg


The rectangle need not be aligned with the grid. Accept slight inaccuracies in drawing provided the intention is clear.

Q2.
Shows a correct quadrilateral, eg
-


## OR


or
Shows a quadrilateral with an area of $24 \mathrm{~cm}^{2}$ but not a perimeter of 26 cm , eg
-


## OR

- 


! Shading omitted
Accept provided the quadrilateral drawn is unambiguous
! Lines not ruled or accurate
Accept slight inaccuracies in drawing provided the pupil's intention is clear

Q3.
(a) 14
(b) C

## Accept 5

Q4.
Shape drawn on grid as shown:


Accept: shape in any position or orientation.
Accept: slight inaccuracies in drawing provided the intention is clear.
Accept: alternative unambiguous indications of the correct shape provided the intention is clear.
Accept: mathematically correct answers involving fractions of a hexagon.
Shape need not be shaded.

## Ready for a challenge***

Q1.
Award TWO marks for the correct answer of 64
If the answer is incorrect, award ONE mark for evidence
of appropriate working, eg
$48 \div 3=16$
$16 \div 4=$ wrong answer
Calculation must be performed for the award of ONE mark.
Up to 2 (U1)

Q2.
Award TWO marks for two different answers as shown:
5 and 2 or 2 and 5
AND
3.5 and 3.5

If the answer is incorrect, award ONE mark for any one of the above answers.
The two answers may be given in either order.
Do not accept '5 and 2' AND '2 and 5' for two marks.
Up to 2

## Q3.

299

Q4.
(a) E
(b) $B$

Q5.
Award TWO marks for the correct answer of 54
If the answer is incorrect, award ONE mark for evidence of appropriate working, eg
$8 \times 4=32$
$3 \times 4=12$
$5 \times 2=10$
$32+12+10=$ wrong answer
Working must be carried through to reach an answer for the award of ONE mark.

Q6.
(a) 84
(b) Award TWO marks for the correct answer of 5.

If the answer is incorrect, award ONE mark for an appropriate calculation such as:

- $(34-6-8) \div 4=$ incorrect answer.

